

Name:

Solutions / Answers

1. Find  $\frac{dy}{dx}$  for the function  $y = x^3 - x^2 + x - 1$

$$\frac{dy}{dx} = 3x^{3-1} - 2x^{2-1} + x^{1-1} - 0 = 3x^2 - 2x + 1$$

2. Find  $f'(x)$  for the function  $f(x) = \frac{x^3}{3} + \frac{x^2}{2} - x$

$$f'(x) = \frac{3x^2}{3} + \frac{2x}{2} - 1 = x^2 + x - 1$$

3. Find  $y'$  for the function  $y = 75$

$$y' = 0$$

4. Find  $f'(x)$  for the function  $f(x) = -x$

$$f'(x) = -1$$

5. Find  $\frac{dy}{dx}$  for the function  $y = mx + b$

$$\frac{dy}{dx} = m$$

6. Find  $y'$  for the function  $y = \frac{1}{x} + \frac{1}{x^2} = x^{-1} + x^{-2}$

$$y' = -x^{-1-1} + -2x^{-2-1} = -x^{-2} - 2x^{-3} = \frac{-1}{x^2} - \frac{2}{x^3}$$

7. Find  $\frac{dy}{dx}$  for the function  $y = \sqrt{x} + \sqrt[3]{x} - 100 = x^{\frac{1}{2}} + x^{\frac{1}{3}} - 100$

$$\frac{dy}{dx} = \frac{1}{2} x^{\frac{1}{2}-1} + \frac{1}{3} x^{\frac{1}{3}-1} = \frac{1}{2} x^{-\frac{1}{2}} + \frac{1}{3} x^{-\frac{2}{3}} = \frac{1}{2x^{\frac{1}{2}}} + \frac{1}{3x^{\frac{2}{3}}} = \frac{1}{2\sqrt{x}} + \frac{1}{3\sqrt[3]{x^2}}$$

8. Find  $f'(x)$  for the function  $f(x) = x^{-4} - 2x^{-5}$

$$f'(x) = -4x^{-5} + 10x^{-6} = \frac{-4}{x^5} + \frac{10}{x^6}$$

9. Find  $y'$  for the function  $y = (3x^2 + x)(2\sqrt{x} - 5)$

$$y' = (6x + 1)(2\sqrt{x} - 5) + (3x^2 + x)(2 \cdot \frac{1}{2} x^{-\frac{1}{2}})$$

10. Find  $\frac{dy}{dx}$  for the function  $y = \frac{3x^2 - 4}{\sqrt{x}}$

$$\frac{dy}{dx} = \frac{(6x)(\sqrt{x}) - (3x^2 - 4)(\frac{1}{2} x^{-\frac{1}{2}})}{(\sqrt{x})^2}$$

11. Find  $f'(x)$  for the function  $f(x) = (x-1)^4(x+5)^3$

$$f'(x) = 4(x-1)^3(x+5)^3 + (x-1)^4(3)(x+5)^2$$

12. Write an equation for the line normal to the graph of  $f(x) = \frac{(x-1)^3}{(x+2)^2}$  at  $x = -1$

$$f'(x) = \frac{3(x-1)(x+2)^2 - (x-1)^3(2)(x+2)}{(x+2)^4}$$

13. Suppose that  $u(x)$  and  $v(x)$  are functions that are differentiable at  $x=1$  and that  $u(1)=5$ ,  $u'(1)=-3$ ,  $v(1)=-1$ , and  $v'(1)=2$ . Find the values of the following derivatives at  $x=1$ .

$$a. \frac{d}{dx}(uv) = u'v + uv' = u'(x)v(x) + u(x)v'(x)$$

$$\begin{aligned} \text{at } x=1 \quad \frac{d(uv)}{dx} &= u'(1)v(1) + u(1)v'(1) \\ &= (-3)(-1) + (5)(2) \\ &= 13 \end{aligned}$$

$$b. \frac{d}{dx}\left(\frac{u}{v}\right) = \frac{u'v - uv'}{v^2} = \frac{u'(x)v(x) - u(x)v'(x)}{(v(x))^2}$$

$$\text{at } x=1 \quad \frac{d}{dx}\left(\frac{u}{v}\right) = \frac{u'(1)v(1) - u(1)v'(1)}{(v(1))^2} = \frac{(-3)(-1) - (5)(2)}{(-1)^2} = -7$$

14. Write an equation for the line tangent to the graph of  $f(x) = 3x^2 - 4x + 2$  at  $x = -1$ .

$$f(-1) = 3(-1)^2 - 4(-1) + 2 = 3 + 4 + 2 = 9 \quad (x, y) = (-1, 9)$$

$$f'(x) = 6x - 4$$

$$f'(-1) = 6(-1) - 4 = -10$$

$$m = -10$$

Tangent Line Equation

$$y - 9 = -10(x - (-1))$$

$$y - 9 = -10(x + 1)$$